Entropy Regularized Deconvolution of Cellular Cryo-Transmission Electron Tomograms

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Cryo-electron tomography (cryo-ET) allows for the high resolution vi-

2 sualization of biological macromolecules. However, the technique is

Iimited by a low signal-to-noise ratio (SNR) and variance in contrast

at different frequencies, as well as reduced Z resolution. Here, we

5 applied entropy regularized deconvolution (ER DC) to cryo-electron

6 tomography data generated from transmission electron microscopy

7 (TEM) and reconstructed using weighted back projection (WBP). We

 $_{\rm 8}$ $\,$ applied DC to several $\mathit{in \ situ}$ cryo-ET data sets, and assess the re-

9 sults by Fourier analysis and subtomogram analysis (STA).

Cryo-Electron Tomography | Deconvolution | Subtomogram Analysis | Structural Biology | Missing Wedge

 ${\displaystyle R}$ eccent advances in cryo-electron tomography (cryo-ET), most notably the ability to thin cryo-preserved specimens 1 2 using a focused ion beam (FIB), have opened windows for 3 the direct visualization of the cell interior at nanometer-scale resolution (1-9). Cells are rapidly frozen to achieve a vitreous 5 form of ice that preserves biological molecules in a near-native 6 state. They are then cryo-FIB milled to a suitable thickness of 7 100-350 nm for imaging with transmission electron microscopy 8 (TEM). A series of projection images is acquired, typically 9 with 1-5 degree increments and then reconstructed into a 3D 10 volume (10). This 3D reconstruction is rendered for display 11 and analysis, which may entail segmentation to highlight ex-12 tended structures or averaging of sub-volumes for enhancement 13 of molecular-scale resolution (11, 12). 14

While cryo-ET offers unparalleled resolution of cellular 15 interiors, it is challenging for a number of reasons. First, 16 vitrified biological samples are highly sensitive to damage by 17 the electron irradiation required for imaging. Constraints on 18 the permissible exposure result in limited contrast and a low 19 signal to noise ratio (13). Second, the modality of wide-field 20 21 TEM depends on defocus to generate useful phase contrast, 22 but with a non-trivial dependence on spatial frequency that is expressed in a contrast transfer function (CTF). Contrast is 23 lost at low spatial frequencies and oscillates at high spatial fre-24 quencies, meaning that material density could be represented 25 as intensity either darker or lighter than background (14–16). 26 Post-processing is applied to correct this representation in the 27 image intensities. The correction is inherently approximate, 28 29 and is especially challenging in tomography where the defocus varies across the field of view (17). Third, the available raw 30 data are never sufficient to produce an unambiguous recon-31 struction. The tilt range is restricted by the slab geometry, 32 typically to about 120° around the vertical. The projected 33 thickness of a slab also increases with tilt angle, resulting 34 in degraded contrast and resolution from these contributions 35 to the reconstruction. The missing information is best rec-36 ognized in Fourier space, where it is known as the missing 37



Fig. 1. Tilt series collection and the missing wedge issue. Left: Schematic of tiltseries collection scheme. Sample projections are acquired over a range of tilt angles, typically from -60° to $+60^{\circ}$. Right: Middle slice of the kxkz plane shows the missing wedge (MW) and baby missing wedges (BMW) of information visualized in Fourier space.

wedge. The gaps between discrete tilt angles also leave small 38 missing wedges as seen in Fig. 1. Since the reconstruction is 39 equivalent to an inversion in Fourier space, it is obvious that 40 some interpolation is required and that the data are incom-41 plete. As such, it is not surprising that different algorithms can 42 generate somewhat different reconstructions from the same 43 data. Commonly recognized artifacts are elongation along the 44 Z direction and streaks projecting from high contrast points 45 into neighboring planes in the volume. 46

In addition to the missing wedges, TEM images require a significant defocus to get adequate contrast. For *in situ* cryo-ET data, a typical defocus of at least $5 \,\mu\text{m}$ is used. Finally, the process of reconstruction by weighted back projection (WBP) introduces well-known problems. These include significant intensity above and below the sample volume, where we expect

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Significance Statement

Cellular cryo-electron tomography suffers from severely compromised Z resolution due to the missing wedges of information not collected during the acquisition of tilt series. This paper shows that application of entropy regularized deconvolution (ER DC) to TEM tomography, substantially fills in this missing information, allowing for improved Z resolution and better interpretation of cellular structures.

J.S. and E.V. designed the project, E.V. lab acquired data, M.C. and J.S performed data processing and analysis. E.V., J.S., M.E., M.A., Z.K. and D.A. gave insightful input at different stages of the project. M.C. and J.S. wrote the paper with input from all authors.

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vacuum with no signal. This is due to cross-terms in the WBP 53 coming from the tilt wedges, as well as distortions in the WBP 54 arising from the missing wedge. Because of these issues with 55 cryo-ET data, filters to improve contrast and compensate for 56 57 the missing wedge are an area of ongoing research (18). These 58 techniques include non-linear anisotropic diffusion (NAD), convolutional neural networks based on detector noise models, 59 wavelet based filtering methods, different implementations 60 of deconvolution, and model based iterative reconstruction 61 (MBIR) (19–28). Here, we present a deconvolution approach to 62 achieve both enhanced SNR and missing wedge compensation. 63

The image distortions resulting from the incomplete tilt 64 series and CTF can be characterized in terms of a single sam-65 ple point of the data. This model is referred to as the point 66 spread function (PSF), of which the hour-glass PSF in light 67 microscopy is a classical example (29-31). Formally, the PSF 68 is convolved with all points in the specimen function to form 69 what is recorded in the image (32). If the PSF is well defined, 70 it becomes possible to partially reverse the process of convo-71 lution to obtain an improved reconstruction. This reversal is 72 referred to as deconvolution, which is a mathematical/compu-73 74 tational iterative inversion processing procedure, extensively utilized in astronomy, spectroscopy, and light microscopy to 75 partially restore data distorted by the imaging process (32). 76 The deconvolution process is constrained. The most common 77 constraint is the imposition of positivity of the deconvolved 78 data (32). Other stabilizing constraints may include smooth-79 ing in real space to suppress high-frequency oscillations. DC is 80 also very sensitive to noise, and most DC algorithms include 81 regularization parameters whose values are difficult to evaluate 82 theoretically. Additionally, in most cases the DC algorithms 83 will diverge with increasing iterations, building up mottle and 84 noise that obscure the interpretation of the final DC image. 85 Finally, most DC implementations do not have a practical 86 87 estimate of the error in the converged solution.

Entropy-regularized deconvolution ER-DC (33) is formu-88 lated to handle data with a weak signal to noise ratio, with a 89 regularization term that exploits certain characteristics spe-90 cific to images originating from cell organelles. Specifically, in 91 cellular images, high intensities and high second-order deriva-92 tives exhibit certain sparse distribution, and this property is 93 exploited by the custom regularization used in ER-DC. This 94 95 regularization was originally designed for fluorescence images, and this approach was taken recently for processing of STEM 96 cryo-tomography (CSTET) reconstructions (26). It is similar 97 to deconvolution applied to fluorescence microscopy, where out 98 of focus light creates a haze, but differs in that the artifacts 99 to be removed originate primarily in the reconstruction rather 100 than the optics. Whereas the individual 2D image is treated 101 102 as a bona fide 2D projection, the kernel of the deconvolution was taken as the sum of the illumination profiles used in the 103 tilt series. However, since TEM is currently the dominant 104 modality for biological 3-D imaging of cells (34) and its CTF 105 is complex, this deserves a separate study, which is the focus 106 of this paper. The major distinction is that the contrast in-107 versions, which were absent in the STEM data as acquired for 108 tomography, should be accommodated in construction of the 109 3D PSF for TEM tomography. 110



Fig. 2. Generating the TEM Point Spread Function. (A) Synthetic tilt series of a centered point source. (B) Point source tilt series convolved with CTF. (C) Slice of the weighted back projection tomogram of convolved CTF-point source (PSF), xz view. (D) 3D FFT of tomogram showed in C, xz slice.

Results

Electron Tomography Point Spread Function. The key to a 112 meaningful deconvolution is that the synthetic PSF should 113 represent as closely as possible the 3D image of an ideal point 114 source. In the case of TEM, this requires an accounting for the 115 defocus imposed in the image acquisition, which is customarily 116 expressed in terms of a contrast transfer function (CTF). 117 The 3D PSF for deconvolution was computed from simulated 118 projections of a point source with the same dimensions and 119 pixel spacing as the aligned tilt series (Fig. 2A). The CTF 120 was first convolved with a projected point-source (Fig. 2B), 121 and then a synthetic tilt series was reconstructed to the same 122 dimensions as the original tomogram using the tilt angles 123 represented in the corresponding reconstruction (Fig. 2C). 124 This is the real-space PSF, whose 3D FFT serves as the optical 125 transfer function, or kernel, for the deconvolution (Fig 2D). 126 In principle, the 2D original CTFs vary with the gradient of 127 defocus of the reconstructed volume. For simplicity, in this 128 first demonstration we limited the analysis to a single nominal 129 defocus and a spatially-invariant deconvolution kernel. A flow 130 diagram for the PSF process is shown in (SI Appendix Fig. 131 S1). 132

Tomogram Deconvolution. As a first demonstration of the 133 TEM deconvolution we used a HEK cell cultured on-grid that 134 had been FIB-milled to 150 nm thickness. The reconstructed 135 volume contains membranes, microtubules, and a prominent 136 crystalline protein array. The cells were overexpressing human 137 Parkinson's related protein LRRK2-I2020T (35), and the ob-138 served repetitive structure is likely an autophagosome, given 139 its double lipid bilayer structure (36). Contrast is sharp in 140 slices through the XY plane of the tomogram, as expected 141 (blue plane-mid structure, Fig. 3B), but contrast and resolution 142 in the Z direction, seen in a slice through the XZ plane (or-143 thogonal green plane in mid structure, Figure 3C) are severely 144 compromised. Furthermore, the reconstructed volume displays 145 a signal both above and below the specimen when observed 146 in the XZ plane. Since the milled slab of material is finite in 147 the z direction, and the sample is imaged in a vacuum, there 148 should be negligible intensity outside it in the reconstructed 149 data. This is a known artifact of back projection. These image 150 distortions in real space can also be characterized in Fourier 151 space, where the real space dimensions (x, y, z) correspond 152

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Fig. 3. Filling of Missing Wedge by Deconvolution (A) Schematic of slices used to generate panels B, C, I and J. (B)XY Slice of a tomogram of a HEK cell reconstructed using back projection. Throughout this work, white intensities correspond to high density values. (C) XZ slice of the same tomogram. (D) Schematic to show slices through Fourier space used to generate E,G,K,M in blue and F,H,M,L,M in green. (E,G) Slice through 3D FFT of the back projection corresponding to XY shown with a different distribution of voxel intensities . (F,H) Slice through 3D FFT of the back projection corresponding results for the tomogram after deconvolution including a spatial constraint. Scale bars: 100 nm.

to the Fourier dimensions (K_x, K_y, K_z) . The protein array in the real space XY plane appears as a lattice of calculated diffraction spots in the plane (K_x, K_y) , as expected (Figure 3E). In the XZ plane, the lattice of spots is sharply truncated at the Fourier planes normal to the limits of the acquired tilts. In summary, back projection suffers from major distortions visible in both real and Fourier space.

The result of 3D deconvolution processing is shown along-160 161 side the reconstruction in Figure 3. Full details appear in the supporting information. All processing was performed using 162 PRIISM image processing software (37). Briefly, the entropy-163 regularized deconvolution algorithm from PRIISM was applied 164 using the simulated PSF. In addition to imposing a penalty on 165 negative intensities (positivity constraint), a spatial constraint 166 was added to the error function on each iteration in order to 167 penalize for spurious intensity reconstructed above and below 168 169 the specimen volume. While contrast is enhanced in the XY plane, the more striking improvement is seen in the XZ plane 170 (Fig. 3J), in comparison with the back projection (Fig. 3C). 171 In the deconvolved tomogram, two lipid bilayers are visible 172 (arrow) across the entire sample along Z, as is the crystalline 173 array (Fig. 3J). The restoration of information along Z in 174 real space can also be seen in the 3D Fourier transform of 175 the deconvolved volume, which shows increased signal in the 176 previously empty regions corresponding to the missing wedges 177

(Fig. **3**F,L).

A very effective way to observe the results of DC is to 179 study a small volume of the WBP and/or DC in a dynamic 180 interacting display module, typically a video of the rotating 181 volume. Stereo pairs with additional rotated views are shown 182 for the WBP and DC (SI Appendix videos 1 and 2). These 183 may be rocked with a cursor bar, as described in supporting 184 information, in order to gain an impression in 3D. Distortions 185 along the Z axis associated with the WBP are largely removed 186 after DC processing, with a visual improvement in resolution 187 along Z. Resolution in the deconvolution can be esti-188 mated by analysis of the Fourier transform as shown 189 by the data (Figure S2). Significant information appears 190 in the power spectrum appears beyond a spatial frequency 191 of approximately 2.5 nm, which corresponds nominally to the 192 second zero in the CTF for 6 micron defocus. 193

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A Second Deconvolution Example. For a second example, we 194 applied ER-DC to a tomogram of a relatively thick lamella of S. 195 *cerevisiae* cells (370 nm). Besides the thickness, cryo-electron 196 tomography data of nuclei are challenging samples to interpret 197 as nuclei are densely packed, and lack high-contrast features 198 like membranes and cytoskeletal elements. As with the DC of 199 mammalian cells, DC provided increased contrast in XY and 200 an improved ability to visually interpret information along 201



Fig. 4. Deconvolution of a Tomogram of the Nuclear Periphery of a Yeast Cell. (A) Central slice (10.62 nm thick) of the XY plane of a WBP tomogram of the nuclear periphery of a *S. cerevisiae* cell. (B) Fourier transform of A. (C) Central slice of the XZ plane of a WBP tomogram. (D) Fourier transform of C. (E) Central slice of the XY plane of a the tomogram from A, deconvolved with a smoothing parameter of 1e2 and a non-linearity factor of 10,000. (F)Fourier transform of E. (G) Central slice of the XZ plane of the XY plane of a the tomogram from E. (H) Fourier transform of G.(I) 10.6 nm slice of the XZ plane of a the tomogram from A, deconvolved with a smoothing parameter of 1e2 and a non-linearity factor of 10,000. (J)Fourier transform of I. (K) 10.6 nm slice of the XZ plane of the deconvolved tomogram from I. (L) Fourier transform of K. Scale bars: 100 nm

Z compared to the back projection. The nuclear envelope is 202 clearly visible in the XY slices of the WBP and the two DCs 203 (Fig. 4 A, E, I). In XZ however, no clear structure can be 204 followed in the BP(Fig. 4C), but can be more easily followed 205 in the DC (Fig. 4 G, K)). Additionally, the missing wedge 206 seen in Fourier space is filled in by the DC process (Fig. 4 H, 207 L)). By utilizing rotating angle stereo-pair renderings of the 208 volume (RAPSs), one can compare the WBP and DC volumes 209 in 3D (SI Appendix videos 3 and 4). In the BP, there is little 210 distinguishable structure as the volume rotates. In contrast, 211 fine features can be identified at every angle, such as the 212 nuclear envelope, as well as densities that could correspond to 213 214 chromatin and nucleosomes. The 3D-FFT of the DC (Fig. 4), KxKz view, shows the missing wedges being filled in, indicating 215 that the DC process helps correct for these artifacts, even in 216 challenging samples. 217

Deconvolution and Subtomogram Analysis. Subtomogram analysis is an approach to protein structure determination *in situ* (11, 38–52). Similarly to single particle analysis, of
which it is an extension to 3D, averaging multiple examples of identical images serves to reduce noise. 3D averaging can

also be used to compensate for the missing wedge in a given 223 tomogram acquisition if the molecules lie in random orienta-224 tions (11). The crystalline-like body seen in Fig. 3 provided 225 an interesting test case for averaging where orientations were 226 determined uniformly by translational symmetry in the crystal 227 (Fig. 5). Therefore only select orientations are available for 228 view. First, we attempted to align the crystal subunits over 229 360° in θ and ϕ on the WBP reconstruction. This resulted 230 in an average that was dominated by the missing wedge, a 231 common pitfall in sub-tomogram averaging, and produced a 232 structure that was strongly elongated in the view direction 233 (Fig. 5A). Second, we used the same particles, but this time 234 from the deconvolved data set, aligned and averaged them with 235 a resulting structure that resembled much better the unit of 236 the crystalline array in the original tomogram (Fig. 5E). Third, 237 we averaged the WBP particles using the DC alignment trans-238 formations. In this last case, we obtained a structure similar to 239 the one obtained from DC-aligned and DC-averaged particles 240 (SI Appendix Fig. 4B). This is a very practical realization 241 of the improved axial resolution in the DC, or equivalently 242 the suppression of the missing wedge artifact in the WBP 243 data, demonstrating that the alignment of subtomograms is 244



Fig. 5. Back projection vs deconvolution crystal body averages. (A) Two views of the crystal body average of WBP subtomograms. (B) Central 3.5nm slice of WBP crystal body subtomogram average. (C) 3D-FSC curves generated from two half-map averages of the WBP crystal body subtomogram average. Green line is the average, pink lines are individual directional FSCs. D) 3D render of directional FSC curves. (E-H) corresponding averages and FSCs derived from the DC volume. Scale bars: 10 nm

improved by DC. This tomogram was acquired from a HEK
cell overexpressing human LRRK2 (35). While the identity
of the molecules forming the crystalline-like array was not
specifically established (e.g., by CLEM) and the number of
particles in this tomogram is severely limited (82), the DC average resembles the cryo-EM structures of LRRK2 determined
both *in situ* bound to microtubules (35) and *in vitro* (53).

Fourier shell correlation (FSC) is widely used in single par-252 ticle cryo-EM (54), as a metric of the resolution of a molecular 253 structure. It is a quantitative measure of similarity, typically 254 implemented in cryo-EM by comparing two structures, each 255 generated from a half dataset. Standard FSC compares global 256 similarities, giving a single curve for the entire structure, show-257 ing the correlation score as a function of spatial frequency. 258 Resolution is then quoted as the inverse spatial frequency 259 where the correlation drops below an accepted threshold. Di-260 rectional FSC (dFSC) is a variant in which all Euler angles are 261 explored for frequency comparison, and provides a represen-262 tation of resolution in all directions (55). dFSC was applied 263 to two half-map averages of the crystalline arrays from the 264 WBP, and then to the DC averages to assess any change in 265 resolution in any direction between the WBP (Fig. 5 C) and 266 DC (Fig. 5G). Both averaged correlation curves drop to near 267 zero by a frequency of 1/.02 Å⁻¹), implying a resolution on 268 the order of 5 nm. However there is a striking difference in the 269 degree of anisotropy as a function of direction in the WBP; 270 in the DC curves most of the directional correlation lines run 271 nearly parallel. This is also reflected in the isosurfaces shown 272 in Figure 5D and H. 273

To investigate the effects of DC in the alignament of the 274 particles and the improvement of the average due to the miss-275 276 ing wedge separately, we chose to use microtubules, since their structure is well established, as are the pipelines for 277 subtomogram analysis. We analyzed a tomogram of recon-278 stituted microtubules decorated by the Parkinson's related 279 protein LRRK2^{RCKW}(53). In the tomogram, it is evident that 280 the deconvolution process increased the contrast between the 281 microtubules and the surrounding media, and we again see 282 a reduction in XZ distortions (Fig. 6A,B,D,E), as well as a 283 corresponding filling of information in the missing wedge in 284

Fourier space (Fig. 6C, F). Microtubule subtomograms were 285 extracted from both the WBP and DC volumes using the 286 filament tracing function in Dynamo(56). The subtomograms 287 were independently aligned and averaged as described in (35)288 (Fig. 7 A, B). Note that the contrast between protofilaments 289 is distinctly sharper for the DC data. However, this method of 290 alignment includes an azimuthal randomization that is specif-291 ically designed to cancel out the missing wedge in the final 292 average. To assess the effect of DC specifically on the missing 293 wedge, we also ran the alignment on particles without this 294 randomization step. Compared to the WBP, the DC-processed 295 average shows more distinctly visible protofilaments in the 296 direction of the missing wedge (Fig. 7E). Last, we used the DC 297 alignment parameters to average the WBP particles (Fig. 7F). 298 Here, the average still shows a prominent missing wedge. Thus, 299 the DC improves both the alignment and the averaging steps 300 of subtomogram analysis. 301

Discussion

We have successfully applied ER DC to cryo-electron tomo-303 grams, and demonstrated enhanced contrast compared to the 304 back projection reconstructions, as well as less distorted struc-305 tures along the Z axis. In real space, one can follow membranes 306 in the XZ plane of the deconvolved volume, that were hardly 307 visible in the back projection. In Fourier space, it is clear 308 that portions of the missing wedge are filled in, and the distri-309 bution of voxel intensities changes significantly as a result of 310 deconvolution. However, there are still several considerations 311 for TEM deconvolution, and these are further discussed in the 312 supporting information. 313

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First, the reality is that DC acts as a filter for the data. 314 The intensity of each voxel is modified in some fashion, and 315 care must be taken in interpreting the DC volume. DC has two 316 parameters, for non-linearity and smoothness, and the optimal 317 values must be determined experimentally by systematically 318 varying the parameters over several orders of magnitude; the 319 parameter search quickly settles into basic convergent DC im-320 ages that look biologically reasonable (e.g. membrane bilayers 321 are visible, ribosomes are distinct, etc.) At the end of the DC 322 process, one can usually settle on a few DC images coming 323



Fig. 6. Deconvolution of a tomogram of reconstituted microtubules. (A) XY slice of the WBP-reconstructed tomogram containing microtubules. (B) XZ view of the tomogram in A; blue dashed line in A corresponds to the slice shown. (C) kxkz view showing the missing wedge. (D) XY of the deconvolved tomogram. (E) XZ of deconvolved microtubule tomogram in D; blue dashed line in D corresponds to the slice shown. (F) kxkz of the deconvolved tomogram. Scale bar = 50 nm

from a close smoothness parameter. These different DC images are studied side-by-side comparing 3-dimensional volumes for details. The side-by-side images are very similar to one another, but subtle features between them exist. Crucial are the orthogonal Z image planes for judging smoothness parameters and structure. There are a number of considerations for the DC process, discussed in the supporting information.

How does one know if the DC structure is credible? In 331 addition to the side-by-side study of several smoothness DC 332 images, a control raw WBP image must be studied alongside 333 the DC images, at several intensity scalings of the WBP data. 334 Any feature uncovered in the DC data would be searched for 335 in the raw WBP data control, and would have to be present 336 in the WBP control. However, in our experience, the DC 337 process has never been observed to invent a structure that is 338 not present in the WBP raw data control. (26). 339

This study makes the statement that the missing wedge 340 of information is substantially filled by DC. Visually and in 341 Fourier space representation this is the case; however, this 342 statement needs caution. We do not know if DC will improve 343 Z resolution for certain kinds of data, intensities, or different 344 structures *e.g.*, of various sizes. It is possible that spaced 345 periodic structures position on top of one another along Z in 346 a tomogram are not resolved correctly in the DC data. 347

A second point in the DC discussion centers on what mathematics allows unobserved data to propagate from areas of observed data, into their correct structural space. Since all im-350 age information can be decomposed into 3-dimensional Fourier 351 representation, one is, in essence, saying that there is informa-352 tion in one region of Fourier space that can be extrapolated 353 correctly into other regions of Fourier space by the DC process. 354 There are two examples from the inverse problems literature 355 to reassure that such extrapolated information can indeed 356 be real. The first one is called "Analytical Continuation" 357 ((57)), and references therein), which is known in optics liter-358 ature. The Analytical Continuation (AC) conjecture, taken 359 from (57), states: All image information can be decomposed 360 into a Fourier transform, and a spatially bounded region of 36 Fourier space can be expressed as an analytical function. The 362 analytical function can be exactly known for a small region, 363 and if there is no noise, the entire analytical function can be 364 determined/extrapolated by AC. The extension can continue 365 indefinitely, and this is a hallmark of AC (57). Noise is critical 366 and the analytical values become small as iterations progress 367 as the function get extended to higher resolution regions of 368 Fourier space, reasons AC is little used (but see (57)). In 369 the case of ER DC, noise is heavily suppressed and resolution 370 extensions required are modest, suggesting that AC might 371 work. 372

The second one is called compressive sensing reconstruction, 373 used in modalities such as magnetic resonance imaging (58)374 and tomography (59). It involves high-quality reconstruc-375 tion from highly under-sampled Fourier data and tomographic 376 projections with a limited set of angles with regularization con-377 structed using derivatives. Because of the way the derivative 378 operator is related to the measurement operator (tomographic 379 projection or Fourier transformation), high quality reconstruc-380 tion becomes possible from sparse Fourier samples or from 381 tomographic projections from a limited set of angles. Although 382 these theories are not directly extensible to our recovery prob-383 lem, these theories reassure that extensions in Fourier space 384 are possible, and hence the filled-in missing wedges may be 385 trusted if the resultant structures in the real space appear 386 plausible. 387

Another independent argument supporting why the missing wedges could correctly be filled can be given from a statistical viewpoint. Recall that the regularization used in the ER-DC



Fig. 7. Subtomogram analysis of WBP and DC-processed microtubule. In all panels, top and side views of the average are shown for the microtubule average obtained under the specified conditions (A) Average from the WBP tomogram, using a randomized azimuth-angle (ϕ) averaging approach to compensate for the missing wedge (35). (B) Average from the DC tomogram using the same randomized ϕ scheme. (C) Average from the WBP tomogram, with initial constant ϕ angles for all particles, allowing the missing wedge to affect the average. (D) Average from the DC tomogram using the same constant]*phi* scheme. (E) Average generated by applying the alignment parameters from the DC uniform starting azimuth/restricted rotation alignment to the the WBP particles. (F) Schematic showing the location of the slice on the right-hand side image in each panel. Scale bars: 10 nm.

enforces certain hypothesized joint distribution of intensity 391 and second-order derivative magnitude. It turns out that the 392 back projected images deviate significantly from this joint dis-393 tribution. Hence, the minimization involved in ER-DC brings 394 395 in a proper filling on the wedges such that: 1) the resulting 396 real space image is consistent with the measured projections, and 2) the resulting real space image better matches with 397 hypothesized distribution. 398

Thirdly, DC could have an impact on the electron dose 399 required to obtain a suitable tomogram. Because only one 400 tilt axis for the tomogram is necessary to largely fill in the 401 missing wedges, multi-axis tilt schemes meant to minimize the 402 missing wedge become unnecessary. The DC process might 403 allow other dose reduction steps, such as fewer tilts and lower 404 beam intensity. In addition, there are several aspects of the 405 DC process that can be improved, and are described in the 406 supporting information. 407

The DC process filling in the missing wedges in Fourier 408 409 space allows biological structures to be followed in 3dimensions. This resolution is adequate to see, for example, 410 gaps between the 10 nm nucleosomes allowing a chromosome 411 path to be followed. One imagines a two step process for cellu-412 lar tomography: first, the path of a structure is followed with 413 the architecture discerned, a process greatly improved by DC. 414 Subsequently, once an architecture is determined, molecular 415 features can be superimposed using averaging methods and 416 molecular modelling (35). 417

418 Materials and Methods

Sample Preparation. Yeast S. cerevisiae W303a cells were 419 grown at 30°C in YPD media (1% yeast extract, 2% bac-420 421 topeptone, and 2% glucose) to mid-log phase, after which $5-\mu L$ were deposited in a glow-discharged Quantifoil grid (200-422 mesh copper R2/1, Electron Microscopy Sciences), followed 423 by manual blotting and plunge freezing in a 50/50 ethane 424 propane mix (Airgas) using a custom-built manual plunger 425 (Max Planck Institute of Biochemistry). Human Embryonic 426 (HEK-293T) cells transfected with LRRK2-I2020T cells were 427 prepared as described in (35). In vitro reconstituted LRRK2-428 I2020T was prepared as described in (53). For both yeast and 429 HEK cells, frozen cells were micromachined on a Scios or an 430 Aquilos 2 DualBeam FIB/SEM microscope (TFS). FIB milling 431 was done as described in (6). 432

433 Cryo-electron tomography. Tilt series were obtained on a 434 300 kV Tecnai G2 Polara (TFS) or Titan Krios with a field emission gun, a GIF Quantum LS energy filter (Gatan) and a 435 K2 Summit $4k \times 4k$ pixel direct electron detector (Gatan). Tilt 436 series were acquired between $\pm 50^{\circ}$ and $\pm 70^{\circ}$ with increments 437 of 2° and 3° , total electron doses between 70 and 100 e⁻/Å² 438 at a target defocus of 5μ m, and a pixel size of 2.2 or 3.5Å 439 using the SerialEM software (60) in low-dose mode. Bidi-440 rectional or dose-symmetric tomography acquisition schemes 441 were used (61), corrected for the pretilt of the lamella where 442 appropriate. Images acquired on the K2 detector were taken 443 in counting mode, divided into frames of 0.075 to 0.1 s. 444

Tomogram Reconstruction. Tilt series were aligned and doseweighted by cumulative dose with MotionCorr2 (62). Doseweighted tilt series were aligned and reconstructed using
Etomo, part of the IMOD package (63). Patch tracking was

used to define the model for fine alignment. The aligned tilt 449 series were reconstructed using weighted back projection to generate the 3D tomograms. 451

Deconvolution. A set of synthetic projections was generated 452 with x and y dimensions and pixel spacing matching the re-453 constructed volume that will be deconvolved. Each projection 454 has a centered point source that is then convolved with the 455 inverse Fourier transform of the CTF, generated using the 456 defocus and astigmatism parameters estimated by CTFFIND4 457 (17). The convolved point source/CTF is then reconstructed 458 using the same elliptically weighted back projection used to 459 generate the target reconstructed volume. Finally, the recon-460 struction is cropped to the same dimensions as the volume 461 to be deconvolved, the 3D FFT of which will be used as the 462 final PSF. Deconvolution is then run for 100 cycles using the 463 PSF generated. A detailed description of the deconvolution 464 procedure can be found in the supporting information. 465

Subtomogram Analysis. Microtubules filaments were traced in 466 Dynamo to define coordinates and orientation. Single particles 467 were defined every 4 nm along the filament, and subtomograms 468 with a side length of 66 nm were then extracted from both 469 the back projected and the deconvolved tomograms using 470 these coordinates. For both sets of particles, subtomograms 471 were iteratively aligned over three rounds of two iterations 472 each. The particles were aligned using a spherical alignment 473 mask to minimize bias. For the first round, the alignment 474 was constrained to a 180 degree cone aperture, with no flip 475 allowed and 20 degrees of azimuthal rotation, corresponding 476 to the third Euler angle. Rounds two and three used a 30 477 and 10 degree cone aperture, respectively, and an azimuthal 478 search range of 10 and 2 degrees respectively. No symmetry 479 was assumed in the alignment. For further details, see (35). 480 To assess any compensation for the missing wedge, alignment 481 was performed on particles with initial tables describing the 482 particles orientation from 1) a blank table to set all particle 483 orientations to zero, and 2) a random table assigning each 484 particle a random orientation. 485

To calculate averages for the autophagosome crystal sub-486 unit in the WBP and DC tomograms, first 50 particles were 487 identified manually in the deconvolved volume to generate an 488 initial average. This initial average was used as a template 489 for Dynamo's template matching functionality and used to 490 search for similar particles. A cross correlation threshold of 491 0.38 was selected, below which many particles appeared as 492 false positives by visual inspection. Using the coordinates and 493 putative orientations from template matching, 82 particles 494 were cropped from both the back projected and deconvolved 495 volumes. A global alignment was used on each dataset in two 496 (even and odd sets) using the Dynamo subtomogram alignment 497 function. Each half dataset was averaged and the directional 498 Fourier shell correlation (dFSC) between the resulting half-499 averages. The alignment angles from the deconvolved particles 500 were then applied to the back projection particles to create 501 the average shown in Fig. 5A and to the relative resolution by 502 dFSC. 503

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